

3.3. Recursive parsing

LL(1)-grammar

- Let us observe the following grammar G :

$$\begin{aligned} E &\rightarrow T + E \mid T - E \mid T \\ T &\rightarrow a \mid (E) \end{aligned}$$

- Modify the productions of E to get an equivalent grammar G' :

$$\begin{aligned} E &\rightarrow TE' \\ E' &\rightarrow +E \mid -E \mid \epsilon \\ T &\rightarrow a \mid (E) \end{aligned}$$

- The leftmost derivations of the strings of G' can easily be formed from the start symbol E : In every phase of parsing the *next* character of the string uniquely determines the production which has to be selected.
- Grammar with this property is called *LL(1)-grammar* ("left to right scan, producing left parse with 1 symbol lookahead")

Recursive parser for LL(1)-grammar

- The parser (parsing program) consists of recursive functions that correspond the nonterminal variables.
- The parser for G' :

```
function  $E$ 
```

```
begin
```

```
  do something;
```

```
   $T$ ;
```

```
   $E'$ ;
```

```
end
```

```
function  $E'$ 
```

```
begin
```

```
  if ( $next == '+'$ ) then
```

```
    begin
```

```
      do something;
```

```
       $next = getnext$ ;
```

```
       $E$ ;
```

```
    end
```

```
  else
```

```
    begin
```

```
      if ( $next == '-'$ ) then
```

```
        begin
```

```
          do something;
```

```
           $next = getnext$ ;
```

```
           $E$ ;
```

```
        end
```

```
      else do something;
```

```
    end
```

```
end
```

```
function  $T$ 
```

```
begin
```

```
  if ( $next == 'a'$ ) then
```

```

begin
  do something;
  next = getnext;
  return;
end
else
begin
  if (next == '(') then
  begin
    do something;
    next = getnext;
    E;
    if (next ≠ ')')
      ERROR;
    next = getnext;
  end
  else ERROR;
end
end

```

In the main program:
next = *getnext*;
E;

- The parse of string $a-(a+a)$ when the command "do something" prints the used production:

$$E \rightarrow TE'$$

$$T \rightarrow a$$

$$E' \rightarrow -E$$

$$E \rightarrow TE'$$

$$T \rightarrow (E)$$

$$E \rightarrow TE'$$

$$T \rightarrow a$$

$$E' \rightarrow +E$$

$$E \rightarrow TE'$$

$$T \rightarrow a$$

$$E' \rightarrow \epsilon$$

$$E' \rightarrow \epsilon.$$

The above corresponds the derivation:

$$\begin{aligned} E &\Rightarrow TE' \Rightarrow aE' \Rightarrow a - E \Rightarrow a - TE' \\ &\Rightarrow a - (E)E' \Rightarrow a - (TE')E' \\ &\Rightarrow a - (aE')E' \Rightarrow a - (a + E)E' \\ &\Rightarrow a - (a + TE')E' \Rightarrow a - (a + aE')E' \\ &\Rightarrow a - (a + a)E' \Rightarrow a - (a + a) \end{aligned}$$

The general form of a LL(1) grammar

- In LL(1) grammars we also allow in restricted form
 - Productions which has the right side starting with a product
 - Products A for which $A \Rightarrow^* \epsilon$
- The grammar producing language $a^*b \cup c^*d$:

$$\begin{aligned} S &\rightarrow Ab \mid Cd \\ A &\rightarrow aA \mid \epsilon \\ C &\rightarrow cC \mid \epsilon. \end{aligned}$$

Grammar is LL(1), despite that the firstly used product can not be decided directly looking the products of S

Modifying a grammar to LL(1) form

- LL(1) rather an limited subclass of context free languages
- Whith the following transformations some "almost"LL(1) grammars can be modified to LL(1) form

1. LEFT FACTORING

- Grammar with products

$$A \rightarrow \alpha\beta_1 \mid \alpha\beta_2, \quad \alpha \neq \epsilon, \beta_1 \neq \beta_2$$

can not be LL(1)

- Modification: let us take a new variable A' and replace the above products with the following

$$\begin{aligned} A &\rightarrow \alpha A' \\ A' &\rightarrow \beta_1 \mid \beta_2, \end{aligned}$$

where α is the longest common prefix of $\alpha\beta_1$ and $\alpha\beta_2$

2. REMOVAL IMMEDIATE LEFT RECURSION

- Grammar is *left recursive*, if for some variable A and string γ

$$A \Rightarrow^+ A\gamma,$$

where $\alpha \Rightarrow^+ \beta$ means that β can be derived from α with derivatin having lenght at least one

- Left recursive grammar can not be LL(1)
- *Immediate* left recursion, i.e., the derivations $A \Rightarrow A\gamma$, can be eliminated by replacing products

$$A \rightarrow A\beta \mid \alpha, \quad \beta \neq \epsilon,$$

with

$$\begin{aligned} A &\rightarrow \alpha A' \\ A' &\rightarrow \beta A' \mid \epsilon \end{aligned}$$

- Products of the form $A \rightarrow A$ can be removed