

Alphabet: $\{a, b, c\}$

Probabilities: $\{0.7, 0.2, 0.1\}$.

Entropies: $\{0.51, 2.32, 3.32\}$

Sequence to be compressed: (a, a, b, a, c)

- a. Total code length = $0.51 + 0.51 + 2.32 + 0.51 + 3.32 = \underline{7.19 \text{ bits}}$.
- b. Redundancy is 0.81 bits as we have to round up to nearest integer value, which is 8 bits.
- c. Huffman code: $\{0, 10, 11\}$, resulting to $0010011 = \underline{7 \text{ bits}}$.
- d. Huffman code gives result lower than entropy, which should be impossible! The reason is that the model used is incorrect. The actual probabilities are $\{0.6, 0.2, 0.2\}$ that would result to: $3 \cdot 0.73 + 2 \cdot 2.32 = \underline{\mathbf{6.85 \text{ bits}}}$.